Evaluating Product Spreading Characteristics on Rotational Rheometer Using the Power Law Model

Introduction

The rheological properties of a product can influence how it is visually and texturally perceived by a consumer and how it is likely to behave during product use. For example, very shear thinning materials will be highly responsive to changes in applied stress while Newtonian materials will show much lesser dependence. Such a response is important when considering the ease of spreading or 'spread-ability'.

The process of spreading causes a consequent reduction in the layer thickness as it is distributed over a wider surface area as shown in Figure 1. Since shear rate is equal to the applied velocity divided by the layer thickness, spreading can therefore not be attributed to a single shear rate.

A better way of assessing spread-ability is by characterizing the change in viscosity over a range of shear rates as shown in Figure 2. The region of interest is the shear thinning or power law region since this describes how easily the material structure breaks down with applied shear. This region appears linear on a log-log plot of viscosity vs. shear rate with a constant gradient, but shows power law dependence when plotted on a linear scale.
APPLICATION NOTE Evaluating Product Spreading Characteristics on a Rotational Rheometer Using the Power Law Model

Mathematically this region of the flow curve can be described using the Power Law or Ostwald de Waele Model given by Equation 1.

\[ \sigma = k\gamma^n \]

- \( k \) is the consistency
- \( n \) is the power law index
- \( \sigma \) is the shear rate

Consistency has the units of Pas\(^n\) but is numerically equal to the viscosity measured at 1 s\(^{-1}\). The power law index ranges from 0 for very shear thinning materials to 1 for Newtonian materials.

The lower the stress input required the easier the material should be to spread. A lower value of \( k \) means lower viscosity and hence lower stress input, while a lower value of \( n \) indicates greater shear thinning which translates to a smaller stress increase with increasing shear rate.

This information can be represented on a chart similar to that shown in Figure 3. Materials with low \( k \) values and/or low \( n \) values should be easiest to spread.

Experimental

- The spread-ability of a number of consumer products was evaluated by performing a shear rate ramp test and analyzing the resultant curve using a power law model.
- Rotational rheometer measurements were made using a Kinexus rotational rheometer with a Peltier plate cartridge and a roughened parallel plate measuring system\(^1\), and using standard pre-configured sequences in the rSpace software.
- A standard loading sequence was used to ensure that both samples were subject to a consistent and controllable loading protocol.
- All rheology measurements were performed at 25°C.
- The flow curve was generated using a shear rate ramp test and a power law model fitted to this curve.

![Diagram showing how different products may fit on a plot of k versus n](image)
APPLICATION NOTE Evaluating Product Spreading Characteristics on a Rotational Rheometer Using the Power Law Model

Results and Discussion

Figure 4 shows the viscosity-shear rate curve for a number of commercial products and their corresponding fitting parameters, with graphical presentation of the latter in Figure 5.

Although toothpaste and hand cream have similar $k$ values, hand cream has a much lower $n$ value making it more shear thinning and easier to spread. Conversely, syrup and chocolate sauce have much lower $k$ values but are not shear thinning hence they appear thick and sticky during application. The body lotion has both a relatively low $k$ and $n$ value making it much easier to apply.

To quantitatively compare the stress requirement for the spreading of a hand cream and syrup respectively at equivalent shear rates the values of $n$ and $k$ can be substituted into Equation 1. Considering a single shear rate of $1 \text{ s}^{-1}$ which may equivocate with a thicker product layer than the stress required to maintain flow at this shear rate is $279 \text{ Pa}$ for the hand cream and $10 \text{ Pa}$ for syrup ($\sigma = k$ at $1 \text{ s}^{-1}$). At a shear rate of $1000 \text{ s}^{-1}$ which would relate to a thinner layer of material resulting from the spreading process the stress requirement increases to $734 \text{ Pa}$ for the hand cream and $10,000 \text{ Pa}$ for the syrup. This highlights importance of non-Newtonian behavior in the spreading process.

Flow curves and model fitting parameters for various samples

Model fitting parameters $k$ and $n$ plotted against one another
APPLICATION NOTE Evaluating Product Spreading Characteristics on a Rotational Rheometer Using the Power Law Model

Conclusion

A shear rate ramp test with a power law model fit was used to characterize the spread-ability of various commercial products using the power law fitting parameters $k$ and $n$. Low values of $k$ and $n$ indicate lower viscosity and a greater degree of shear thinning respectively, which will contribute to easier spreading.

Please note...

that testing is recommended to be undertaken with cone and plate or parallel plate geometry – with the latter being preferred for dispersions and emulsions with large particle sizes. Such material types may also require the use of serrated or roughened geometries to avoid artefacts relating to slippage at the geometry surface.